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International College Penang

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**FINAL
Examination Paper
(COVER PAGE)**

Session : AUGUST 2014

Programmes : Diploma in Electrical and Electronic Engineering (DEEI)

Course : EEE2108 : MODERN CONTROL SYSTEMS ENGINEERING

Date of Examination : December 11, 2014 (Thursday)

Time : 8.00am -10.00am Reading Time: Nil

Duration : 2 Hours

Special Instructions :

This is a supplementary exam paper. This paper consists of SIX (6) questions. Answer any FOUR (4) questions in the answer booklet provided. All questions carry equal marks.

Students are not allowed to remove this question paper from the examination venue.

Materials permitted:

Non-programmable scientific calculator

Materials provided:

Laplace Transform Table (Appendix)

Worksheet for Question 4(b)

Worksheet for Question 4(c)

Examiner(s): Mr. Chan Tse Wei

Moderator: Dr. Ooi Beng Lee

This paper consists of 7 printed pages, including the cover page.

INTI INTERNATIONAL COLLEGE PENANG

DIPLOMA IN ELECTRICAL AND ELECTRONIC ENGINEERING PROGRAMME (DEE/I)

**EEE2108 : MODERN CONTROL SYSTEMS ENGINEERING
FINAL EXAMINATION : AUGUST 2014 SESSION**

Instructions: This paper consists of **SIX (6)** questions. Answer any **FOUR (4)** questions in the answer booklet provided. All questions carry equal marks. Marks for each sub-question are shown in square brackets.

Question 1

a. Reduce the block diagram in Figure-Q1(a) to a single transfer function $T(s) = C(s)/R(s)$ using the following methods:

- i. Block diagram algebra. [6]
- ii. Signal flow graph. [8]

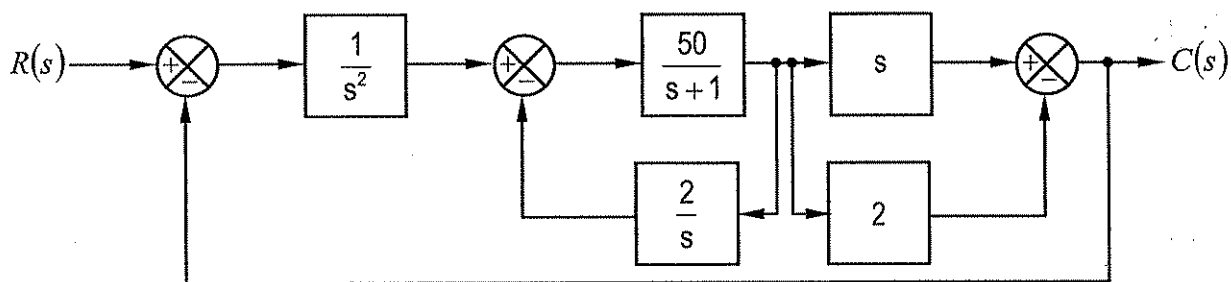


Figure-Q1(a)

- i. Is the system in Figure-Q1(a) stable? [1]
 - ii. Qualitatively justify your answer given in part (b)(i). [2]
- i. Derive the error signal expression, $E(s)$ of the system in Figure-Q1(a), in terms of its input signal, $R(s)$ and the system's transfer function, $T(s)$. [3]
 - ii. Hence, determine the system's steady-state error in response to a unit step input. [5]

Question 2

a. For the system shown in Figure-Q2(a), calculate,

- i. The percent overshoot [7]
- ii. The peak time [3]
- iii. The settling time [3]

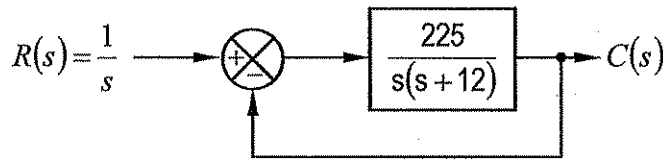


Figure-Q2(a)

Figure-Q2(b)(i) shows the step response of the system in Figure-Q2(b)(ii). Base on the step response, approximate the respective value of *a* and *b*. [12]

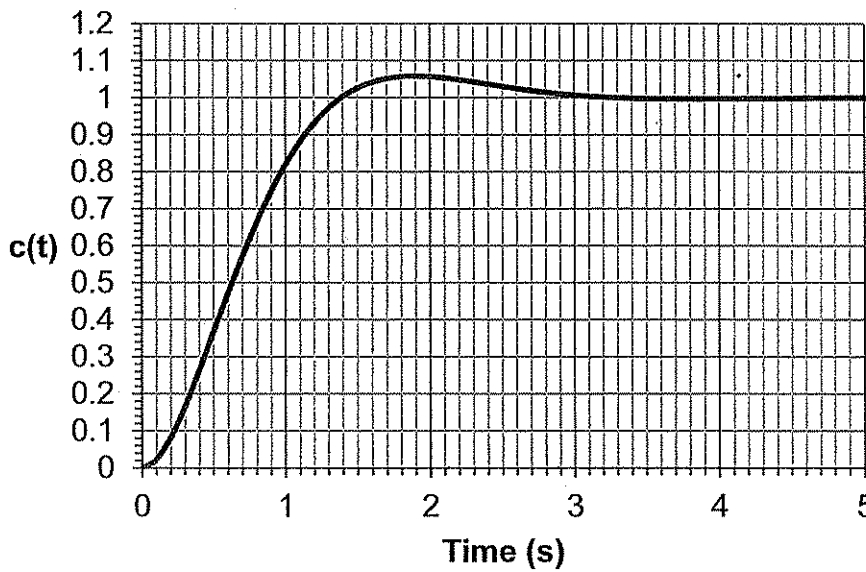


Figure-Q2(b)(i)

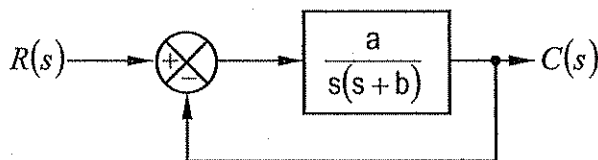


Figure-Q2(b)(ii)

Question 3

- a. State if the following statements are true or false.
- i. A system is stable if the natural response approaches zero as time approaches infinity. [1]
 - ii. A system is stable if the natural response approaches infinity at the initial condition. [1]
 - iii. A system is marginally stable if the natural response neither decays or grows but remains constant or oscillates. [1]
 - iv. A system is stable if every bounded input yields a bounded output. [1]
 - v. A system is unstable if any bounded input yields an unbounded output. [1]
 - vi. System with positive real closed-loop poles is unstable. [1]
 - vii. Repeated poles located along the imaginary axis of the s-plane denote system stability. [1]

- b. A unity negative feedback system has an open-loop transfer function given as,

$$G(s) = \frac{1000}{(s+2)(s+3)(s+5)}$$

- i. Set up the Routh array table for the system. [5]
- ii. Hence, determine if the system is stable. Justify your answer. [3]
- iii. Without calculation, determine the number of closed-loop poles of the system that are located at the left side of the s-plane? [2]

- c. A unity negative feedback system has an open-loop transfer function given as,

$$G(s) = \frac{K}{(s^2 + 2s + 2)(s + 2)}$$

- i. Sketch the Nyquist diagram for the system's open-loop transfer function by setting K to unity and replacing $s = j\omega$, where ω ranges from 0 to infinity. [5]
- ii. From the Nyquist diagram drawn in part (c)(i), justify that when $K = 20$, the system is marginally stable. [3]

Question 4

a. For each of the root loci shown in Figure-Q4(a), explain why the root loci is incorrect. [6]

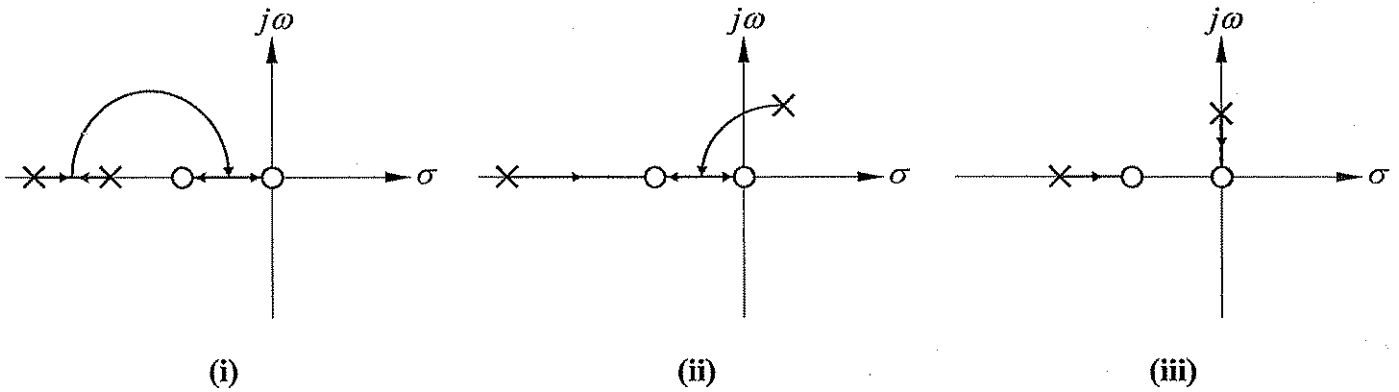


Figure-Q4(a)

b. Sketch the general shape of the root locus for each of the open-loop pole-zero plots shown in Figure-Q4(b). Submit your answer using the accompanying worksheet. [6]

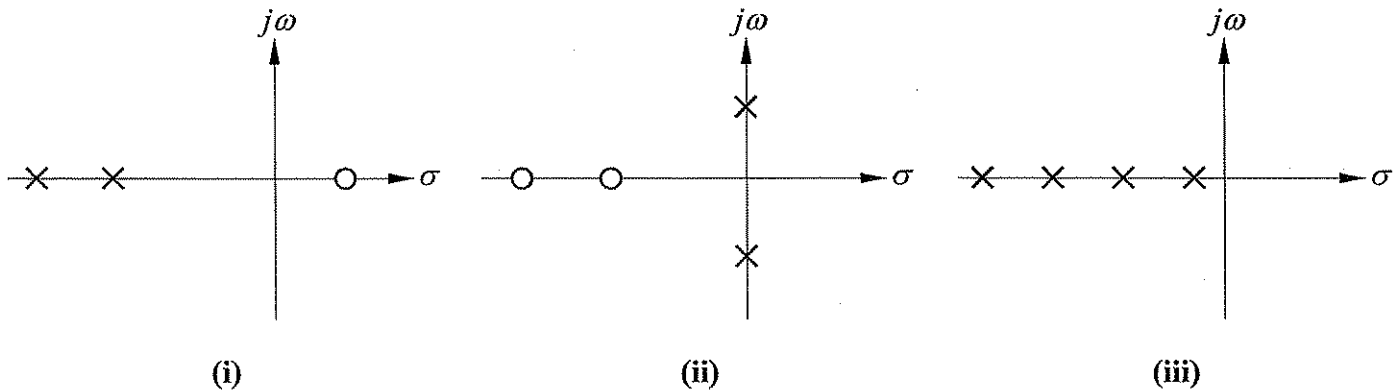


Figure-Q4(b)

c. Figure-Q4(c) shows open-loop poles and zeros drawn on an s-plane. There are two possibilities for the sketch of the root locus. Sketch each of the two possibilities in the accompanying worksheet. [6]

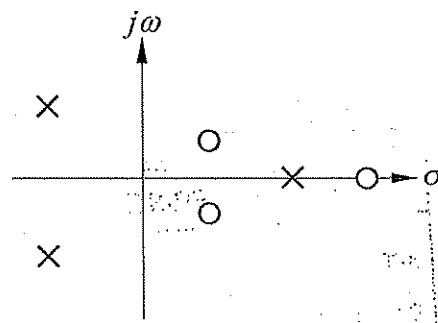


Figure-Q4(c)

d. Figure-Q4(d) shows a root locus plot of a unity negative feedback system.

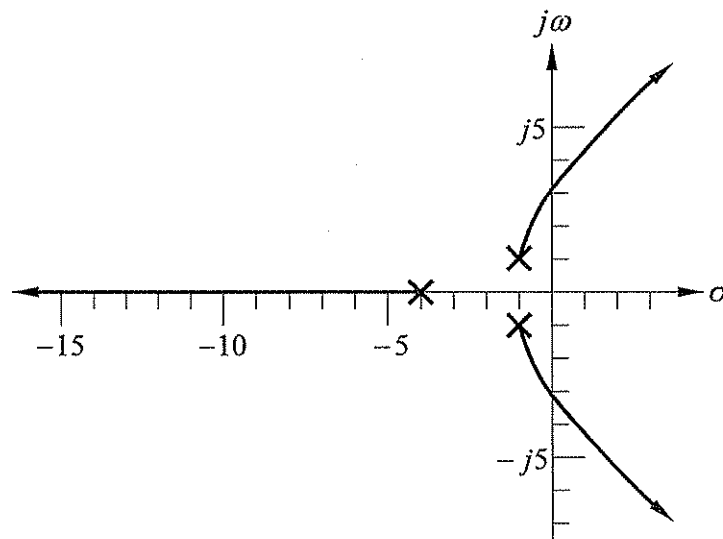


Figure-Q4(d)

- i. Find the value of gain that will make the system marginally stable. [5]
- ii. Find the value of gain for which the closed-loop transfer function will have a pole on the real axis at -5 . [2]

Question 5

The open-loop transfer function of a negative unity feedback system is given as,

$$G(s) = \frac{1}{s(s+2)(s+4)}$$

- a. Express the analytical expression for the magnitude and phase response for $G(s)$. [4]
- b. Sketch the Bode magnitude response for $G(s)$ ranging from $\omega > 0.1$ rad/s, clearly identify the corner frequencies and the corresponding gain values. [9]
- c. Identify the gain crossover frequency of $G(s)$ in rad/s. [4]
- d. Calculate the phase margin of $G(s)$. [4]
- e. Calculate the phase crossover frequency of $G(s)$. [4]

Question 6

- a. The circuit shown in Figure Q6(a) is to implement a compensator. Derive the circuit's transfer function expression and justify that it implement a phase lead compensator. [10]

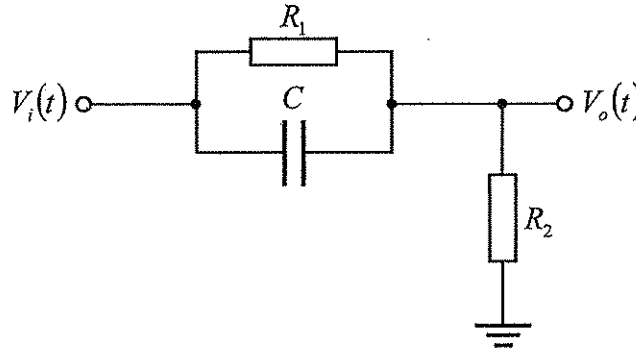


Figure-Q6(a)

- b. The open-loop transfer function of an uncompensated second order control system is given by $G(s) = \frac{2}{s(s+4)}$. Design a phase-lead network for the system such that the response has 10% overshoot for a step input and approximately $\frac{4}{3}s$ of settling time at 2% accuracy. [15]

– THE END –

Appendix-1: THE LAPLACE TRANSFORM TABLE

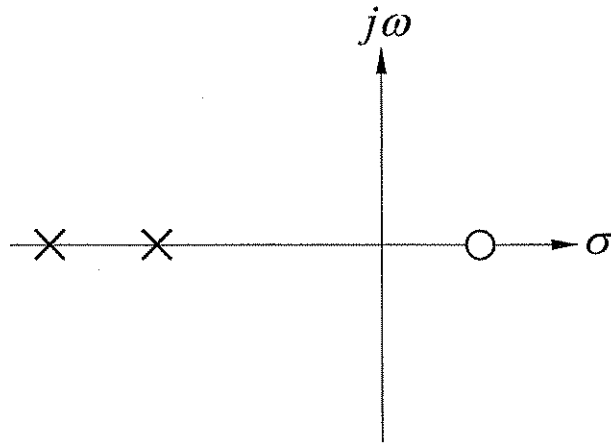
Definition	$f(t)$ from $t > 0$	$F(s) = \mathcal{L}[f(t)] = \int_0^{\infty} f(t)e^{-st} dt$
1. Sum	$af_1(t) + bf_2(t)$	$aF_1(s) + bF_2(s)$
2. First Derivative	$\frac{d}{dt}[f(t)]$	$sF(s) - f(0)$
3. n^{th} Derivative	$\frac{d^n}{dt^n}[f(t)]$	$s^n F(s) - s^{n-1}f(0) - s^{n-2}f'(0) \dots f^{(n-1)}(0)$
4. Definite Integral	$\int_0^t f(u)du$	$\frac{F(s)}{s}$
5. Shift in t	$f(t - kT)$	$e^{-skT} F(s)$
6. Exponential multiplier	$e^{-\alpha t} f(t)$	$F(s + \alpha)$
7. Periodic function (period T)	$f(t)$	$\frac{1}{1 - e^{-sT}} \int_0^T e^{-st} f(t) dt$
8. Initial Value	$\lim_{t \rightarrow 0} f(t)$	$\lim_{s \rightarrow \infty} sF(s)$
9. Final Value	$\lim_{t \rightarrow \infty} f(t)$	$\lim_{s \rightarrow 0} sF(s)$
10. Unit impulse at $t = 0$	$\delta(t)$	1
11. Unit impulse at $t = kT$	$\delta(t - kT)$	e^{-skT}
12. Unit step	$u(t)$	$\frac{1}{s}$
13. Delayed step	$u(t - kT)$	$\frac{e^{-skT}}{s}$
14. Rectangular pulse (duration kT)	$u(t) - u(t - kT)$	$\frac{1 - e^{-skT}}{s}$
15. Unit ramp	$r(t) = t$	$\frac{1}{s^2}$
16. Delayed ramp	$r(t - kT)$	$\frac{e^{-skT}}{s^2}$

Definition	$f(t)$ from $t > 0$	$F(s) = \mathcal{L}[f(t)] = \int_0^{\infty} f(t)e^{-st} dt$
17. n^{th} order ramp	t^n	$\frac{n!}{s^{n+1}}$
18. Exponential decay	e^{-at}	$\frac{1}{s+a}$
19. Exponential growth	$1 - e^{-at}$	$\frac{a}{s(s+a)}$
20. Exponential $\times t$	te^{-at}	$\frac{1}{(s+a)^2}$
21. Exponential $\times t^n$	$t^n e^{-at}$	$\frac{n!}{(s+a)^{n+1}}$
22. Difference of exponentials	$e^{-at} - e^{-bt}$	$\frac{b-a}{(s+a)(s+b)}$
23. Difference of exponentials	$\frac{1}{b-a}(be^{-bt} - ae^{-at})$	$\frac{s}{(s+a)(s+b)}$
24. Sine	$\sin \omega t$	$\frac{\omega}{s^2 + \omega^2}$
25. Phase-advanced sine	$\sin(\omega t + \phi)$	$\frac{\omega \cos \phi + s \sin \phi}{s^2 + \omega^2}$
26. Sine $\times t$	$t \sin \omega t$	$\frac{2\omega s}{(s^2 + \omega^2)^2}$
27. Exponentially decaying sine	$e^{-at} \sin \omega t$	$\frac{\omega}{(s+a)^2 + \omega^2}$
28. Cosine	$\cos \omega t$	$\frac{s}{s^2 + \omega^2}$
29. Phase-advanced cosine	$\cos(\omega t + \phi)$	$\frac{s \cos \phi - \omega \sin \phi}{s^2 + \omega^2}$
30. Cosine $\times t$	$t \cos \omega t$	$\frac{s^2 - \omega^2}{(s^2 + \omega^2)^2}$
31. Exponentially decaying cosine	$e^{-at} \cos \omega t$	$\frac{s+a}{(s+a)^2 + \omega^2}$

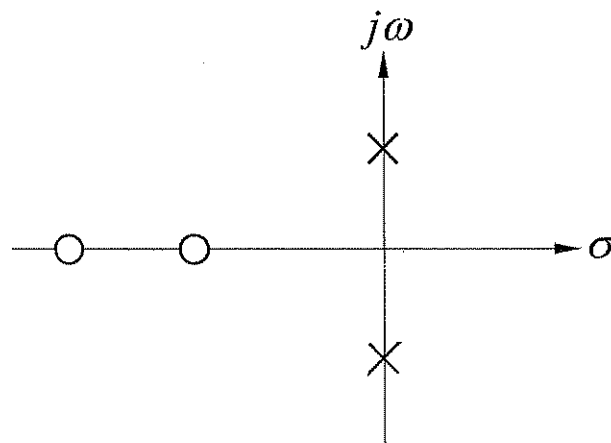
Worksheet for Question 4(b)

Student Name: _____

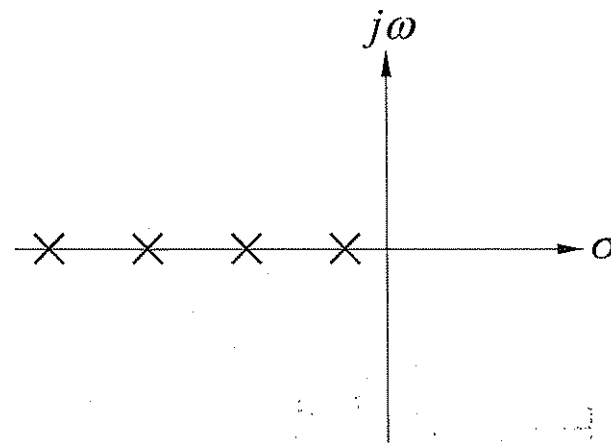
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(i)



(ii)

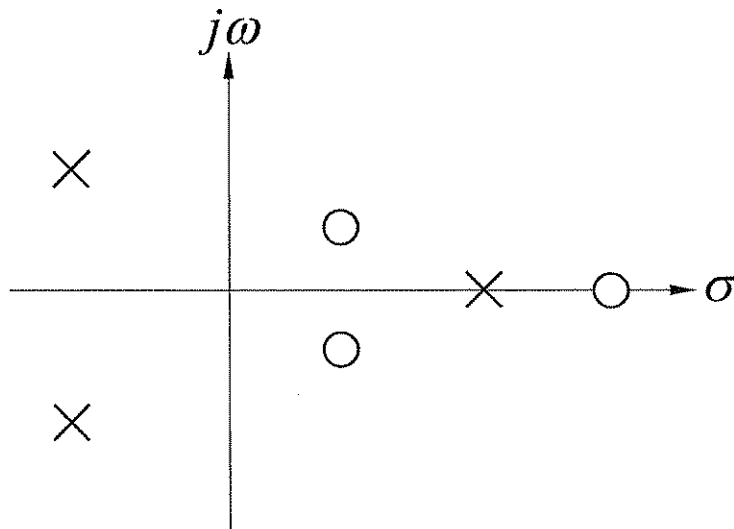


(iii)

Worksheet for Question 4(c)

Student Name: _____

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Possibility 1:**Possibility 2:**