

INTI
International College Penang
 LAUREATE INTERNATIONAL UNIVERSITIES'

FINAL
 Examination Paper
 (COVER PAGE)

Session : August 2017

Programme : Diploma in Electrical and Electronic Engineering (DEEI)

Course : MAT1134: Engineering Mathematics 1

Date of Examination : 9 December 2017 (Saturday)

Time : 2:00pm – 4:00pm Reading Time : Nil

Duration : 2 Hours

Special Instructions :

This paper consists of FIVE (5) questions. Answer any FOUR (4) questions in the answer booklet provided. All questions carry equal marks.

Materials permitted :
Non-Programmable Calculator

Materials provided :
Formula Booklet 1 & Polar Graph Paper (last page of the question paper)

Examiner(s) : Chong Mee Teng

Moderator : Dr. Ch'ng Pei Eng

This paper consists of 6 printed pages, including the cover page.

INTI INTERNATIONAL COLLEGE PENANG

DIPLOMA IN ELECTRICAL & ELECTRONIC ENGINEERING PROGRAMME
 MAT 1134: ENGINEERING MATHEMATICS 1
 FINAL EXAMINATION: AUGUST 2017 SESSION

Instructions: This paper consists of **FIVE (5)** questions. Answer any **FOUR (4)** questions in the answer booklet provided. All questions carry equal marks.

Question 1

(a) Solve the following equations:

(i) $3^{2x+1} - 26(3^x) - 9 = 0$ (5 marks)

(ii) $\sqrt{4x-9} + 1 = 2\sqrt{x}$ (4 marks)

(b) Express $\frac{2\sqrt{7}}{\sqrt{7}+2}$ as a single fraction with rational denominator. (3 marks)

(c) The polynomial $f(x) = 3x^3 + 2x^2 - bx + a$ is divisible by $(x-1)$ but leaves a remainder of 10 when divided by $(x+1)$. Calculate the values of a and b , hence solve the polynomial. (6 marks)

(d) Find the range of values of k for which the equation: $(x+1)^2 + p - 16 = 0$ has real roots. (3 marks)

(e) Express $y = 3x^2 - 4x + 5$ in the form $y = 3(x-p)^2 + q$ where p and q are constants. Find the value of p and q . Hence, sketch the graph of $y = 3x^2 - 4x + 5$. (4 marks)

Question 2

(a) Solve the equation $2 \tan^2 x + 5 \tan x - 3 = 0$ for $0^\circ \leq x \leq 360^\circ$. (7 marks)

(b) Prove that $\cos^2 x (\operatorname{cosec}^2 x - \cot^2 x) \equiv \cos^2 x$. (5 marks)

(c) State the amplitude, period and phase shift of $y = 3 \sin\left(\frac{1}{2}x + \pi\right)$. Hence, sketch the curve for one oscillation. (5 marks)

- (d) Change $(-\sqrt{3}, -1)$ from rectangular coordinates to polar coordinates. (3 marks)
- (e) Sketch the graph: $r = 5 \cos \theta$, $0^\circ \leq \theta \leq 360^\circ$ on the polar axis. (5 marks)

[Please detach the polar graph paper provided from the question paper and tie it together with your answer booklet]

Question 3

- (a) The first term of an arithmetic sequence is 12, the seventh term is 36 and the last term is 144.
- Find the common difference. (2 marks)
 - How many terms are there in the sequence? (2 marks)
- (b) The fifth term of a geometric progression is 48 and the ninth term is 768. All the terms are positive.
- Find the common ratio and the first term. (5 marks)
 - Find the sum of the first ten terms. (2 marks)
- (c) Expand and simplify the first five terms of $(x^2 - 2)^9$ by using the binomial theorem. (3 marks)
- (d) Find the term independent of x in the expansion of $(2x^3 - \frac{1}{x})^{12}$. (5 marks)
- (e) In triangle ABC , $\angle ABC = 110^\circ$, $\angle CAB = 30^\circ$ and $AB = 100$ cm, as shown in the **Figure (1)**.

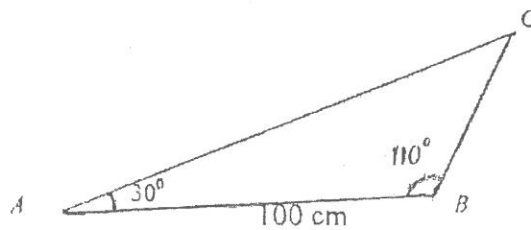


Figure (1)

- Calculate the distance of BC . (3 marks)
- Calculate the area of the triangle ABC . (3 marks)

Question 4

(a) Find $\frac{dy}{dx}$ for each of the following:

(i) $y = x^3 \cos 2x$ (3 marks)

(ii) $y = \frac{e^{2x}}{x - 3e}$ (3 marks)

(iii) $y = \ln\left(\frac{x-1}{2-x}\right)^2$ (3 marks)

(b) Find the equation of tangent to $4x^2 + 2xy^3 - 5y^2 = 0$ at the point (1, 2). (5 marks)

(c) Find the stationary points of the function $y = x^3 - 3x + 5$ and determine the nature of the stationary points. Hence, sketch the graph of the function. (6 marks)

(d) The radius of a circle increases at a constant rate of 0.6 cms^{-1} . Calculate the rate of change in area when its radius is 10 cm. (5 marks)

Question 5

(a) Find the following integrals:

(i) $\int \frac{2}{(2x-3)^3} dx$ (3 marks)

(ii) $\int \cos 4x \cos x dx$ (3 marks)

(iii) $\int_1^2 3e^{2x} + 3 dx$ (3 marks)

(b) Use Simpson's rule with 6 equal intervals to approximate the value of $\int_1^{16} \log(1+x^3) dx$. Show your working in the form of a table and give your final answer to 3 significant figures. (6 marks)

- (c) Use Newton's Method to obtain the root of the equation $e^x + x - 3 = 0$ with the initial value, $x_0 = 1$. Give your answer correct to three decimal places. (5 marks)
- (d) Find the area enclosed by the curves $y = 4x^2$ and $y^2 = 2x$. (5 marks)

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