

## INTI INTERNATIONAL UNIVERSITY

## FOUNDATION IN SCIENCE (CFSI)

## MAT 1210: MATHEMATICS 1

## FINAL EXAMINATION: JUNE 2015 SESSION

Instructions: This paper consists of **FIVE (5)** questions. Answer any **FOUR (4)** questions in the answer booklet provided. All questions carry equal marks.

**Question 1**

a) Find the value of  $(3.25)^{1+\log_{3.25} 10}$  (3 Marks)

b) Express  $\frac{(x^2+1)}{x(x+1)(x-1)}$  in partial fractions. (9 Marks)

c) Evaluate the indefinite integral of  $\int 2x(x^2+10)^{13} dx$  by using u-substitution. (4 Marks)

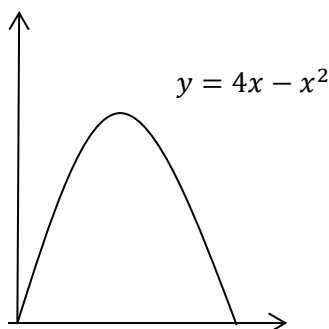
d) Rationalize the denominator of  $\frac{1}{\sqrt{2}+\sqrt{5}}$ . (3 Marks)

e) Prove that  $\frac{\tan \theta + \cot \theta}{\sec \theta \csc \theta} = 1$ . (6 Marks)

**Question 2**

a) By using implicit differentiation, differentiate  $x^2 + y^2 = 4$  with respect to x. (3 Marks)

b) Find the area of the region bounded by the curves of  $y=0$  and  $y=4x-x^2$  as shown in the diagram below. (6 Marks)



- c) Solve  $\frac{(x^3 - 4x^2 + 2x + 5)}{(x + 2)}$  by using long division and write the answers in fractional form. (6 Marks)
- d) Given that the function  $f$  and  $g$  are defined as  $f(x) = px + 3$  and  $g(x) = x + 4p$ .
- i) Given that  $f(2) = g(5)$ , find the value of  $p$ . (4 Marks)
- ii) Find  $fg(x)$ . (2 Marks)
- iii) Solve  $f(x) = g(x)$ . (2 Marks)
- e) Use the factor theorem to determine if  $(2x - 5)$  a factor of  $p(x) = 6x^4 - 15x^3 - 8x^2 + 20x$ . (2 marks)

**Question 3**

- a) Use the binomial theorem to expand  $(3x - y)^3$ . (3 Marks)
- b) Given that the equation of the curve is  $y = 24(3x - 5)^{-2}$ .
- i) Find the gradient of the curve if  $x=2$ . (4 Marks)
- ii) Find the equation of tangent and normal at the point  $(1, 6)$  and gives your answer in the form of  $y=mx+c$ . (7 Marks)
- c) Sketch  $3y + 2x - 12 = 0$  and state the slopes and  $y$ -intercepts. (5 Marks)
- d) Integrate the indefinite integral of  $\int x^3 \ln 3x \, dx$  by using the integration by parts. (6 Marks)

**Question 4**

- a) A point moves along the curve  $y = \sqrt{x^2 + 8}$  in such way that  $\frac{dx}{dt} = 3$ . Find  $\frac{dy}{dt}$  when  $x=1$ . (4 Marks)
- b) Given the equation of the curve is  $y = (x+1)^3 (x+3)^5$ .
- i) Find the gradient of the curve. (3 Marks)
- ii) Find the value of  $\frac{dy}{dx}$  when  $x=4$ . (2 Marks)

- c) By using the factor theorem, find the first root of  $3x^3 - 2x^2 - 17x - 12 = 0$ , then find all other roots by using long division.

(8 Marks)

- d) The function  $f$  is defined by  $f(x) = \frac{kx-5}{m-x}$ ,  $x \neq m$ . If  $f(-1) = -\frac{7}{4}$  and  $f(2) = -1$ . Find the value of  $k$  and  $m$ ;

(8 Marks)

**Question 5**

- a) The line  $y = 4$  and the curve  $y = x^2$  meet at two points.  
i) Find the points of intersection when the region bounded (or enclosed) by the line and the curve is rotated through  $360^\circ$  or  $2\pi$  about the x-axis.

(2 marks)

- ii) Find the volume of the solid generated.

(5 Marks)

- b) Find the coordinates of turning point of  $y = 16x + \frac{1}{x^2}$ . Hence determine the nature of the turning point.

(7 Marks)

- c) Given that  $y = \sin x(1 + \cos x)$ ;

- i) Find the first derivative of the function.

(5 Marks)

- ii) Hence, find the value of  $\frac{dy}{dx}$  when  $x = \frac{\pi}{2}$ .

(2 Marks)

- d) Evaluate  $\int \cos^3 x dx$

(4 marks)

**--THE END--**

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