

FINAL  
Examination Paper

(COVER PAGE)

Session : JANUARY 2018

Programme : FOUNDATION IN BUSINESS INFORMATION  
TECHNOLOGY (CFPI)

Course : **MAT1215 : FUNDAMENTALS OF MATHEMATICS**

Date of Examination : 5 March 2018, Monday

Time : 11:00AM – 1:00PM Reading Time : Nil

Duration : 2 Hours

Special Instructions :

This paper consists of **SIX (6)** questions. Answer any **FIVE (5)** questions in the answer booklet provided. ALL questions carry equal marks

Materials permitted :

Non-Programmable Scientific Calculator

Materials provided :

Formulae Booklet 1 & Graph Paper

Examiner(s) : **Mr. CHAN Ah Wah**

Moderator : **Dr. CH'NG Pei Eng**

*This paper consists of 6 printed pages, including the cover page.*

INTI INTERNATIONAL COLLEGE PENANG  
 FOUNDATION IN BUSINESS INFORMATION TECHNOLOGY (CFPI)  
 MAT1215 : FUNDAMENTALS OF MATHEMATICS  
 FINAL EXAM : JANUARY 2018 SESSION

**Instructions**

This paper consists of **SIX (6)** questions. Answer any **FIVE (5)** questions in the answer booklet provided. All questions carry equal marks. Show complete workings .

**Question 1**

(a) Given that  $A = \left\{ \sqrt{36}, -1.2, \frac{19}{3}, 0, \sqrt{11}, \frac{6}{2}, 1.23, -17, \pi \right\}$ , list down the elements of **A** that belong to the following sets:

- (i) Set of even integer(s)
- (ii) Set of irrational number(s)

[2 marks]

(b) Simplify each of the following expressions:

(i)  $\frac{\frac{x}{y} - \frac{y}{x}}{\frac{1}{y} + \frac{1}{x}}$

[2 marks]

(ii)  $\frac{(x+h)^2 - x^2}{h}$

[2 marks]

(c) Factorize each of the following expressions:

(i)  $x^2 + 4y - xy - 4x$

[2 marks]

(ii)  $8x^2 - 50$

[2 marks]

(d) Rationalize the denominator of  $\frac{\sqrt{3}}{1 - 2\sqrt{3}}$ .

[3 marks]

(e) Simplify  $\frac{(2x^3y^{11})(z^{-5})^4}{5x^{-12}(xz)^{-2}}$  and express your answer in positive exponents only.

[3 marks]

(f) Use scientific notation to simplify  $\frac{(320,000)^2(0.0009)}{12,000^2}$  and write your answer in scientific notation.

[4 marks]

**Question 2**

(a) Find the domain of the following functions:

(i)  $f(x) = \sqrt{3x + 2}$

[2 marks]

(ii)  $f(x) = \frac{x + 1}{x - 5}$

[2 marks]

(b) Find the equation of the line passing through  $(1, -1)$  and parallel to the line  $y = 5x - 2$ .

[3 marks]

(c) Given  $f(x) = -x^2 + 4x - 1$ .

(i) Find the vertex of  $f(x)$ .

[2 marks]

(ii) Find the x and y intercepts. Hence, sketch the graph of  $f(x)$ .

[4 marks]

(d) The total cost of producing a product is given by  $C(x) = 100x + 2000$  and the selling price for each unit is given by  $u(x) = -0.02x + 400$ . Find

(i) the profit function,

[2 marks]

(ii) the marginal profit at  $x = 15$  and interpret your answer,

[3 marks]

(iii) the quantity of the product that has to be produced in order to maximize the profit.

[2 marks]

**Question 3**

(a) Differentiate the following functions with respect to x:

(i)  $y = x - \frac{2}{x^3}$

[2 marks]

(ii)  $y = (1 + 3x)^2$

[2 marks]

(b) Integrate the following functions with respect to x:

(i)  $\int \frac{x^4 + 2x^3 - 1}{x^2} dx$

[2 marks]

(ii)  $\int_1^3 \frac{2}{(3x + 1)^2} dx$

[3 marks]

(c) Find the area enclosed by the curve  $y = 1 - x^2$  and  $y = x - 1$ .

[3 marks]

- (d) Find the 30<sup>th</sup> term of an arithmetic progression in which the fifth term is 13 and the ninth term is 25. [3 marks]
- (e) State the number of terms for the geometric progression 1, 4, 8, ..., 1024. [2 marks]
- (f) Express 4.75757575... as a fraction in its lowest terms. [3 marks]

**Question 4**

- (a) Melvin has invested a sum of money 10 years ago in a savings account that has since paid interest at the rate of 5% per year compounded continuously. His investment is now worth RM2060.90. How much did he originally invest? [3 marks]
- (b) Ahmad invested RM5,000 in a savings account four years ago. His investment is now worth RM12,300. Find the rate of interest per year if the money was compounded quarterly. [5 marks]
- (c) A car costs RM80,000. You pay 10% down payment and amortize the rest with equal monthly payments over a 7 year period. The interest is 9.25% compounded monthly.
- (i) What is the loan amount? [2 marks]
- (ii) What will the monthly payment be? [3 marks]
- (iii) How much is the total interest paid? [2 marks]
- (d) Universal Life offered an annuity that pays 7.25% compounded monthly. If RM1,000 is deposited into this annuity every month, how much is in the account after 15 years? How much is the interest earned? [5 marks]

**Question 5**

- (a) Evaluate the following:

(i)  $\sum_{j=1}^4 \frac{1}{j+1}$  [2 marks]

(ii)  $\sum_{k=1}^3 (3k^2 + 1)$  [2 marks]

(b) Suppose  $\mathbf{A} = \begin{bmatrix} 1 & -1 \\ -5 & -2 \end{bmatrix}$  and  $\mathbf{B} = \begin{bmatrix} -2 & 6 \\ -1 & 4 \end{bmatrix}$ .

Perform the indicated operations below:

(i)  $\mathbf{A+B}$

[2 marks]

(ii)  $\mathbf{AB}$

[2 marks]

(c) Solve the following:

$$\mathbf{X} \begin{bmatrix} 2 & 1 \\ -1 & -1 \end{bmatrix} = \begin{bmatrix} 0 & -1 \\ 2 & -1 \end{bmatrix}$$

[4 marks]

(d) The system of equations below can be written as  $\mathbf{Ax} = \mathbf{b}$ .

$$2x + 3y - 2z = 6$$

$$x - y + 2z = 3$$

$$4x + 2y + 5z = 1$$

(i) List the matrices  $\mathbf{A}$ ,  $\mathbf{x}$ , and  $\mathbf{b}$ .

[3 marks]

(ii) Evaluate  $|\mathbf{A}|$ .

[3 marks]

(iii) Does  $\mathbf{A}^{-1}$  exist? Explain.

[2 marks]

### Question 6

(a) Solve the following linear programming problem graphically:

Maximize :  $P = 7x + 8y$

Subject to :

$$x + 2y \leq 300$$

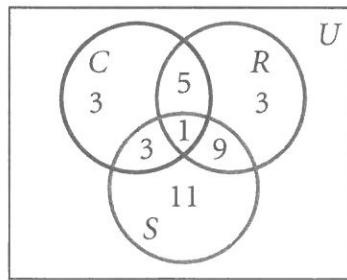
$$3x + 2y \leq 480$$

$$x \geq 0$$

$$y \geq 0$$

[6 marks]

- (b) A group of 9 people consisting of 2 boys, 3 girls, and 4 adults. In how many ways can a team of 4 be chosen if
- both boys are in the team? [2 marks]
  - the adults are either all in the team or all not in the team? [3 marks]
  - at least 2 girls are in the team? [3 marks]
- (c) Given below is the Venn Diagram with 3 interlocking circles labeled as R, C, and S. Answer the following questions:



- How many are in R? [1 mark]
- How many are in R or C? [1 mark]
- How many are in R and S? [1 mark]
- How many are not in C? [1 mark]
- How many are in neither R nor S? [1 mark]
- How many are in C but not in S? [1 mark]

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